



Math Virtual Learning

# HS/Essential Math II

April 27, 2020



High School/Essentials of Algebra Course 2  
Lesson: April 22, 2020(U5L7 Solving Equations One Chunk at a  
Time)

**Objective/Learning Target:**

Student will solve equations using properties of operations and the logic of preserving equality.



## **DIRECTIONS:**

- Scroll through each page
- Read each page
- Attempt each problem on a sheet of paper or in a math notebook/journal

# Bellwork

**I** MysteryGrid **1, 2, 3**

2	3,•	
6,+		
	6,•	

**J** MysteryGrid **4, 5, 6**

20,•		30,•
15,+		
	24,•	

**K** MysteryGrid **2, 3, 5**

20,•		10,+
	45,•	

# Bellwork Answer Key

Ⓘ

MysteryGrid **1, 2, 3**

2 2	3,• 1	3
6,+ 3	2	1
1	6,• 3	2

Ⓙ

MysteryGrid **4, 5, 6**

20,• 4	5	30,• 6
15,+ 6	4	5
5	24,• 6	4

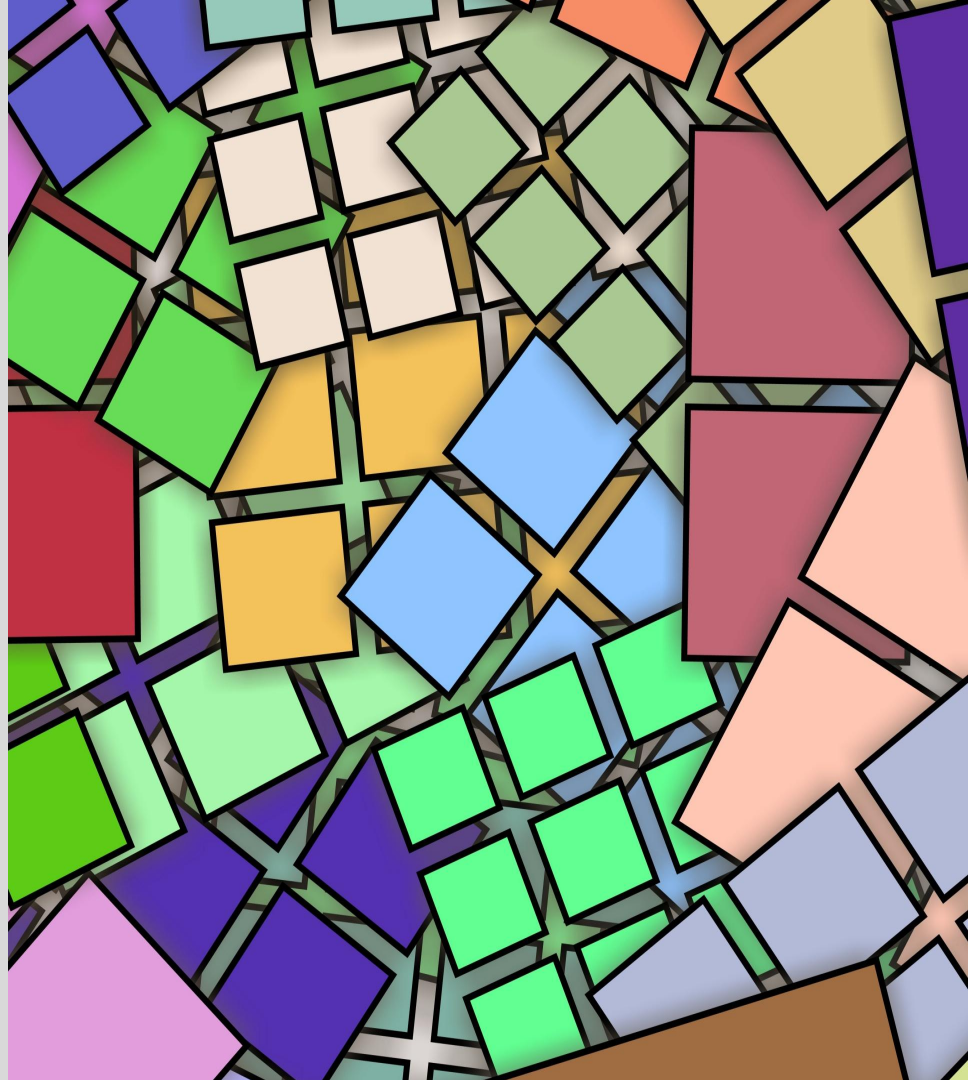
Ⓚ

MysteryGrid **2, 3, 5**




20,• 5	2	10,+ 3
2	45,• 3	5
3	5	2

# Lesson

Solving with Squares



# Guess & Test: Playing with Numbers 0 - 9

⑦ What could , , and  be if all the variables represent different *single-digit* whole numbers?




$$\text{pentagon} \cdot \text{pentagon} = \text{clover}$$

$$\text{pentagon} + \text{pentagon} = \text{moon}$$

$$\text{pentagon} = \underline{\hspace{2cm}}$$

$$\text{clover} = \underline{\hspace{2cm}}$$

$$\text{moon} = \underline{\hspace{2cm}}$$

⑧ What could , , and  be if all the variables represent *different* whole numbers?

$$\text{heart} \cdot \text{apple} = \text{apple}$$




$$\text{apple} \cdot \text{apple} = \text{diamond}$$

$$\text{apple} + \text{apple} = \text{diamond}$$

$$\text{heart} = \underline{\hspace{2cm}}$$

$$\text{apple} = \underline{\hspace{2cm}}$$

$$\text{diamond} = \underline{\hspace{2cm}}$$

⑦ What could , , and  be if all the variables represent different *single-digit* whole numbers?

$$\text{pentagon} \cdot \text{pentagon} = \text{clover}$$

$$\text{pentagon} + \text{pentagon} = \text{moon}$$

$$\text{pentagon} = \underline{3}$$

$$\text{clover} = \underline{9}$$

$$\text{moon} = \underline{6}$$

You need numbers that multiply and sum to different numbers but max out at 9.




$$1 * 1 = 1$$

Cannot work because the product must be different from factors.

$$2 * 2 = 4$$

$$2 + 2 = 4$$

Cannot work because the sum & product cannot equal.

⑧ What could , , and  be if all the variables represent *different* whole numbers?

$$\text{heart} \cdot \text{apple} = \text{apple}$$

$$\text{apple} \cdot \text{apple} = \text{diamond}$$

$$\text{apple} + \text{apple} = \text{diamond}$$

$$\text{heart} = \underline{1}$$

$$\text{apple} = \underline{2}$$

$$\text{diamond} = \underline{4}$$

You need numbers that multiply and sum to different numbers but max out at 9.

1 is the only number you can multiply by and get the same number.

$$2 * 2 = 4$$

$$2 + 2 = 4$$

Cannot work because the sum & product cannot equal.



9

Instructions

Record

Jacob

Lena

Asher

Imani

Carla

Think of a number.		4			-1	
			-3	-1		
	$(b - 1)^2 + 7$	16		8	11	7

9

Instructions	Record	Jacob	Lena	Asher	Imani	Carla
Think of a number.	$b$	4	-2	0	-1	1
Subtract 1.	$b - 1$	3	-3	-1	-2	0
Square the result.	$(b - 1)^2$	9	9	1	4	0
Add 7.	$(b - 1)^2 + 7$	16	16	8	11	7

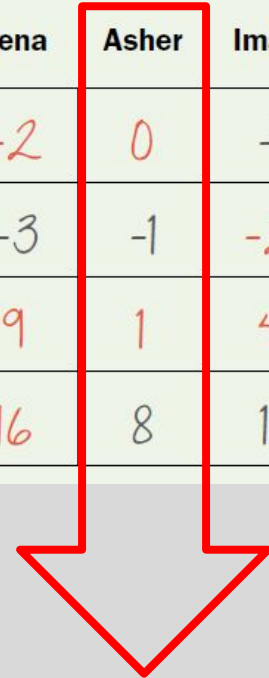
Addition undoes subtraction

Square root undoes squaring

Subtraction undoes Addition

Order of Operations  
What happens first and follows?

Reverse Engineer  
What happens lasts...step by step?



Zero is neither positive nor negative & Positive & negative.

Add 7.

$$(b - 1)^2 + 7$$

16

16

8

11

7

Hiroshi worked through the trick above and got 8 as his final result.  
What two numbers could he have been thinking of?

Hiroshi worked through the trick above and got 8 as his final result.  
What two numbers could he have been thinking of?

$$(b - 1)^2 + 7 = 8$$

$$(b - 1)^2 = 1$$

$$\text{So: } b - 1 = -1 \text{ OR } b - 1 = 1$$

$$b = 0 \quad \text{OR} \quad b = 2$$

Hiroshi was thinking of either 0 (like Asher) or 2.

⑬ Damian thought of a number, subtracted 8, squared the result, and got 49 as his final result. What two numbers could he have been thinking of?

⑭ Maria thought of a number, added 3, squared the result, and subtracted 2. She got 79 as her final result. What two numbers could she have been thinking of?

- ⑬ Damian thought of a number, subtracted 8, squared the result, and got 49 as his final result. What two numbers could he have been thinking of?

(Methods may vary for 14 and 15.)

$$(n - 8)^2 = 49$$

$$n - 8 = 7 \quad \text{OR} \quad n - 8 = -7$$

$$n = 15 \quad \text{OR} \quad n = 1$$

- ⑭ Maria thought of a number, added 3, squared the result, and subtracted 2. She got 79 as her final result. What two numbers could she have been thinking of?

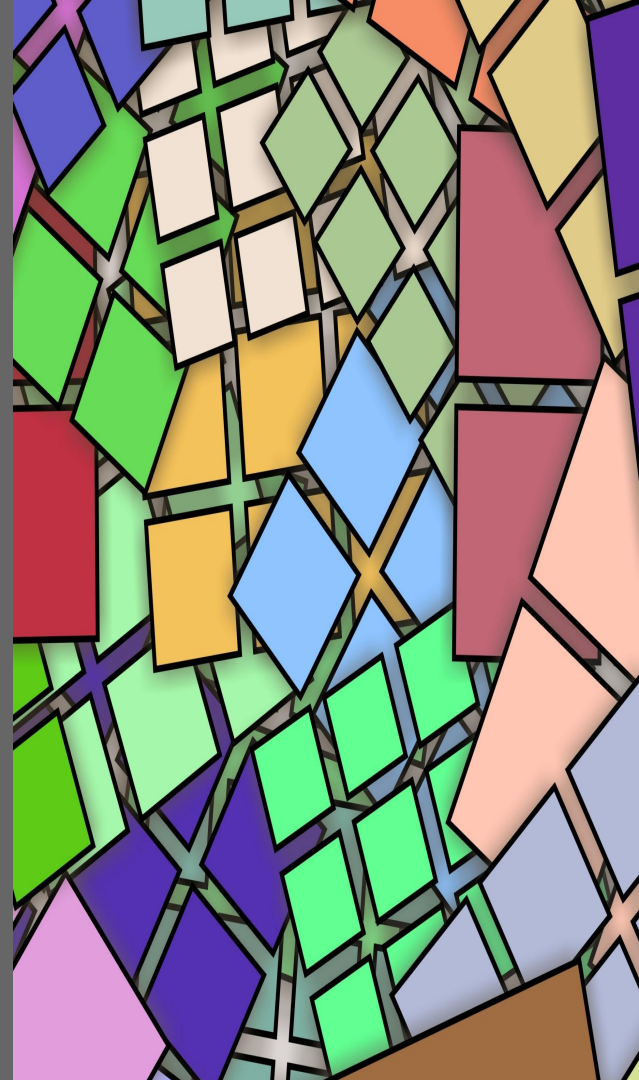
$$(n + 3)^2 - 2 = 79$$

$$(n + 3)^2 = 81$$

$$n + 3 = 9 \quad \text{OR} \quad n + 3 = -9$$

$$n = 6 \quad \text{OR} \quad n = -12$$

**Stuff to Make You Think...**



Click on the link below to practice solving Mystery Grid problems electronically. You should practice until you have solved 2 or 3 puzzles on your own.

<http://www.kenkenpuzzle.com/game>



28

Who Am I?

*h*      *t*      *u*

--	--	--

- I'm not an even number.
- At least two of my digits are even.
- My units digit is half of my tens digit.
- All three of my digits are different.
- My hundreds digit is twice the sum of my units digit and my tens digit.

28

Who Am I?

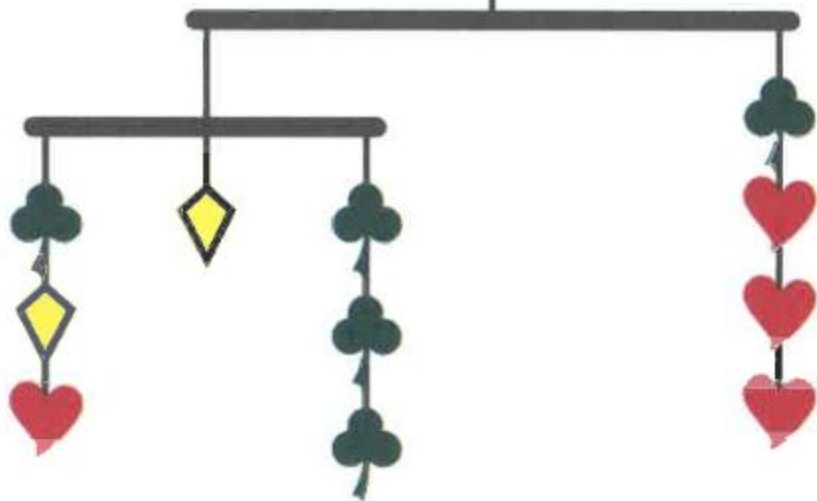
- I'm not an even number.
- At least two of my digits are even.
- My units digit is half of my tens digit.
- All three of my digits are different.
- My hundreds digit is twice the sum of my units digit and my tens digit.


<i>h</i>	<i>t</i>	<i>u</i>
6	2	1

- Not an even means unit is 1,3, 5,7, or 9
- At least two of my digits are even means hundreds and tens are either 0, 2,4,6, or 8 AND hundreds is not zero
- Units is half tens digit means the units is either 1 or 3 and tens is 2 or 6
- Hundreds digit is twice sum of units digit and tens digit means  $h = 2(u+t)$

29

50

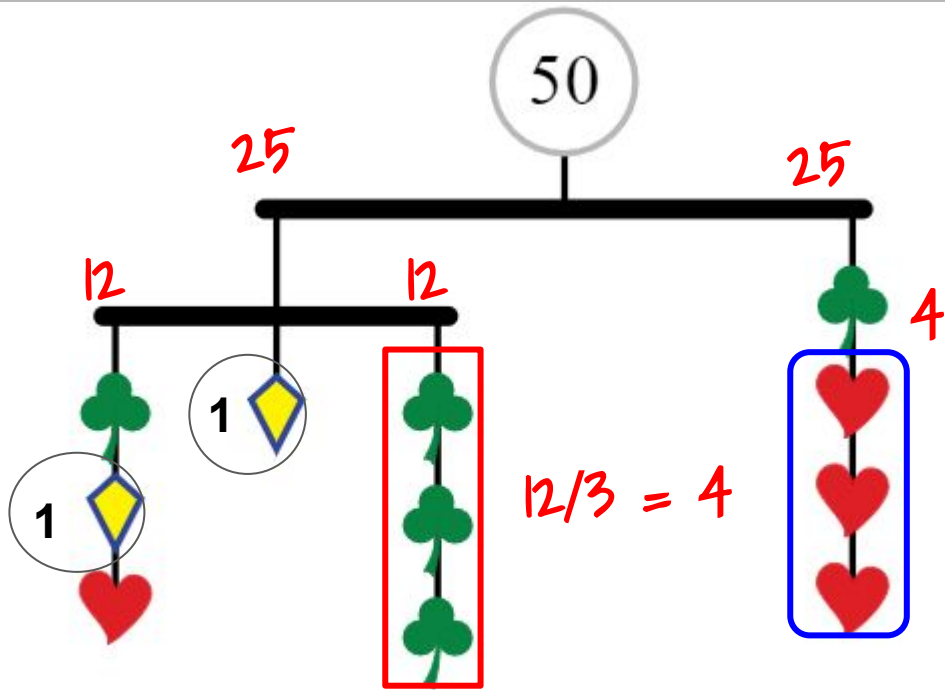



 = \_\_\_\_\_


 = \_\_\_\_\_


 = 1

29



 = 4

 = 7

 = 1

30  $(m + 5)(4m - 7 - 3m) =$  \_\_\_\_\_






31  $(7b + 2c)(5c - 8b) =$  \_\_\_\_\_

30)  $(m + 5)(4m - 7 - 3m) = \underline{m^2 - 2m - 35}$

	$4m$	$-7$	$-3m$
$m$	$4m^2$	$-7m$	$-3m^2$
$5$	$20m$	$-35$	$-15m$

31)  $(7b + 2c)(5c - 8b) = \underline{19bc - 56b^2 + 10c^2}$

	$5c$	$-8b$
$7b$	$35bc$	$-56b^2$
$2c$	$10c^2$	$-16bc$

32) What could , , , , and  be if all the shapes are *different* single-digit numbers (0-9)?

$$\text{yellow circle} \cdot \text{yellow circle} = \text{yellow circle}$$

$$\text{yellow circle} = \underline{\hspace{2cm}}$$

$$\text{red triangle} + \text{red triangle} = \text{red triangle}$$

$$\text{red triangle} = \underline{\hspace{2cm}}$$

$$\text{yellow circle} + \text{green butterfly} = \text{purple heart}$$

$$\text{green butterfly} = \underline{\hspace{2cm}}$$

$$\text{green butterfly} + \text{green butterfly} = \text{blue crescent moon}$$

$$\text{purple heart} = \underline{\hspace{2cm}}$$

$$\text{green butterfly} \cdot \text{green butterfly} = \text{blue crescent moon}$$

$$\text{blue crescent moon} = \underline{\hspace{2cm}}$$

33) Fill in the empty spaces.

	<u>    </u>	<u>    </u>
—	$x^2$	
—	$9x$	$72$

$$(\underline{\hspace{1cm}} + \underline{\hspace{1cm}})(\underline{\hspace{1cm}} + \underline{\hspace{1cm}}) = x^2 + 17x + 72$$

32 What could , , , , and  be if all the shapes are *different* single-digit numbers (0-9)?

$$\text{yellow circle} \cdot \text{yellow circle} = \text{yellow circle}$$

$$\text{orange triangle} + \text{orange triangle} = \text{orange triangle}$$

$$\text{yellow circle} + \text{green butterfly} = \text{purple heart}$$

$$\text{green butterfly} + \text{green butterfly} = \text{blue crescent moon}$$

$$\text{green butterfly} \cdot \text{green butterfly} = \text{blue crescent moon}$$

$$\text{yellow circle} = \underline{1}$$

$$\text{orange triangle} = \underline{0}$$

$$\text{green butterfly} = \underline{2}$$

$$\text{purple heart} = \underline{3}$$

$$\text{blue crescent moon} = \underline{4}$$



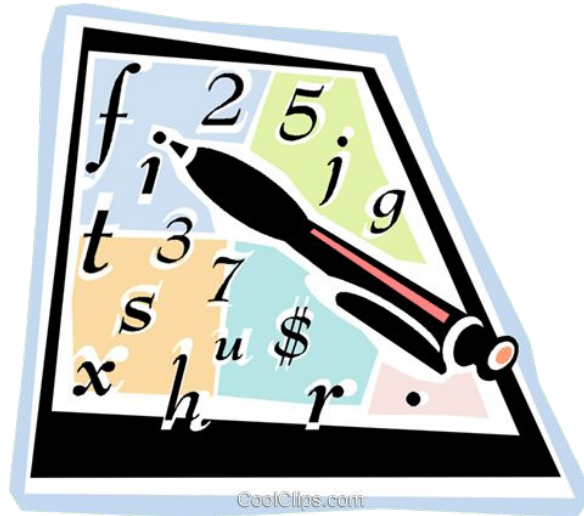
33 Fill in the empty spaces.

	<u>x</u>	<u>8</u>
<u>x</u>	$x^2$	$8x$
<u>9</u>	$9x$	$72$

$$\left(\underline{x} + \underline{9}\right)\left(\underline{x} + \underline{8}\right) = x^2 + 17x + 72$$

or vice versa  $(x + 8)(x + 9)$

# Additional Practice





# Additional Practice 1

$$\textcircled{\text{G}} \quad 5(12 - x)^2 = 45$$

$$\textcircled{\text{H}} \quad \frac{(b + 9)^2}{2} = 8$$

Cover all but the last instruction and the final result to undo each instruction of the trick in reverse order.

# Practice 1 Key

$$\textcircled{G} \quad 5(12 - x)^2 = 45 \quad \frac{45}{5} = 9$$

$$(12 - x)^2 = 9 \quad \sqrt{9} = 3 \text{ or } -3$$

$$\underset{-3}{12 - x} = \underset{-3}{3} \quad \text{OR} \quad \underset{+3}{12 - x} = \underset{+3}{-3}$$

$$x = 9 \quad \text{OR} \quad x = 15$$

$$12 - 9 = 3 \\ x = 9$$

$$12 - 15 = -3 \\ x = 15$$

$$\textcircled{H} \quad \frac{(b + 9)^2}{2} = 8 \quad 8 \times 2 = 16$$

$$(b + 9)^2 = 16 \quad \sqrt{16} = 4 \text{ or } -4$$

$$\overset{-9}{b + 9} = \overset{-9}{4} \quad \text{OR} \quad \overset{-9}{b + 9} = \overset{-9}{-4}$$

$$b = -5 \quad \text{OR} \quad b = -13$$

$$-5 + 9 = 4$$

$$-13 + 9 = -4$$



## Additional Practice 2

- ① Jessica thought of a number, subtracted 7, squared the result, and got 25 as her final result. Find both possibilities for the number she thought of.

# Answer Key 2

- ① Jessica thought of a number, subtracted 7, squared the result, and got 25 as her final result. Find both possibilities for the number she thought of.

$$(n - 7)^2 = 25 \quad \sqrt{25} = 5 \text{ or } -5$$

$$n - 7 = 5 \quad \text{OR} \quad n - 7 = -5$$

$$n = 12 \quad \text{OR} \quad n = 2$$



## Additional Practice 3

- ⓐ Michael thought of a number, doubled it, added 3, squared the result, and got 81 as his final result. Find both possibilities for the number he thought of.

# Answer Key 3

- ① Michael thought of a number, doubled it, added 3, squared the result, and got 81 as his final result. Find both possibilities for the number he thought of.

$$(2n + 3)^2 = 81 \quad \sqrt{81} = 9 \text{ or } -9$$

$$2n + 3^{-3} = 9^{-3} \quad \text{OR} \quad 2n + 3^{-3} = -9^{-3}$$

$$\frac{2n = 6}{2} \quad \text{OR} \quad \frac{2n = -12}{2}$$

$$n = 3 \quad \text{OR} \quad n = -6$$



# Additional Resources

Student will solve equations using properties of operations and the logic of preserving equality.

CLICK THE LINKS BELOW FOR ADDITIONAL PRACTICE:

**[SolveMe Mobiles](#)**

**[Who Am I? Puzzles](#)**

**[Solve Me Mystery Grids](#)**

Mobiles

Mystery  
Grids

Who  
Am I ?